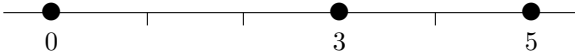
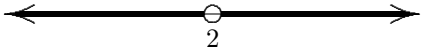



SOLUTIONS TO EXERCISES: MATHEMATICIANS ARE FOND OF COLLECTIONS

IN-SECTION EXERCISES:

1. The object(s) in a set are called the *element(s)* or *member(s)* of the set.
If a set has n members, where n is a whole number, then it is a *finite* set. Otherwise, it is an *infinite* set.
2. The sentence ‘ n is a whole number’ is true when n is chosen from the set $\{0, 1, 2, 3, \dots\}$. Otherwise, the sentence is false.
4. The centered dots denote multiplication.
5. There are 5 members in the set $\{a, b, c, d, e\}$.
There are $5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$ different re-arrangements of the five-member set $\{a, b, c, d, e\}$.
6. Let $T = \{a, b, c, d, e\}$.
7. Let $S = \{7, 8, 9, \dots\}$.
- 8a. T
- 8b. T
- 8c. F
- 8d. T
- 8e. ST/SF
- 10a. EXP, number
- 10b. EXP, set
- 10c. EXP, set
- 10d. SEN, T Read as: ‘5 is a member of the set of real numbers’ or ‘5 is in the set of real numbers’ or ‘5 is an element of the set of real numbers’ or, most simply, ‘5 is a real number’
- 10e. SEN, F Read as: ‘5.1 is a member of the set of integers’ or, most simply, ‘5.1 is an integer’
- 11a. 

A horizontal number line with tick marks at 0, 3, and 5. Solid black dots are placed at each of these three tick marks.
- 11b. 

A horizontal number line with an open circle at the tick mark for 2. Arrows at both ends of the line indicate that the set continues infinitely in both directions.
- 11c. 

A horizontal number line with open circles at the tick marks for 0, 3, and 5. Arrows at both ends of the line indicate that the set continues infinitely in both directions.
- 12a. ‘1 is in the empty set’; false
- 12b. ‘0 is in the empty set’; false
- 12c. ‘0 is not in the empty set’; true
- 12d. ‘ x is not in the empty set’; (always) true
- 13a. EXP, set
- 13b. EXP, set
- 13c. EXP, number
- 13d. EXP, set
- 13e. SEN, F ‘1 is in the the set of real numbers between 1 and 2, including 2 but not including 1’
- 13f. SEN, T ‘1 is in the set of real numbers between 1 and 2, including 1 but not including 2’
14. The subsets of $\{a, b\}$ are: $\{a, b\}$, \emptyset , $\{a\}$, $\{b\}$. There are four subsets.
15. The subsets of $\{0, 2, 4\}$ are: $\{0, 2, 4\}$, \emptyset , $\{0\}$, $\{2\}$, $\{4\}$, $\{0, 2\}$, $\{0, 4\}$, $\{2, 4\}$. There are eight subsets.

- 16a. The set $\{-1, 2, 3\}$ *is* a subset of \mathbb{R} , since every member of $\{-1, 2, 3\}$ is a real number.
16b. The set $\{-1, 2, 3\}$ *is not* a subset of the whole numbers, because -1 is not a whole number.
16c. The set $\{-1, 2, 3\}$ *is* a subset of the integers, since every member of $\{-1, 2, 3\}$ is an integer.
16d. The set $\{-1, 2, 3\}$ *is* a subset of the interval $(-2, \infty)$, since every member of $\{-1, 2, 3\}$ is in the interval $(-2, \infty)$.

END-OF-SECTION EXERCISES:

17. EXP, set
18. SEN, T
19. SEN, T
20. EXP, set
21. SEN, F
22. SEN, T
23. SEN, T
24. $\{-1, 0, 1\}$
25. $(-1, 1]$
26. $[0, 2)$
27. $(-\infty, 1]$
28. $(-1, \infty)$
29. There are eight subsets of $\{-1, 0, 1\}$: $\{-1, 0, 1\}$, \emptyset , $\{-1\}$, $\{0\}$, $\{1\}$, $\{-1, 0\}$, $\{-1, 1\}$, $\{0, 1\}$.
30. The set of positive integers *is* a subset of $(-1, \infty)$, since every positive integer is in the interval $(-1, \infty)$.